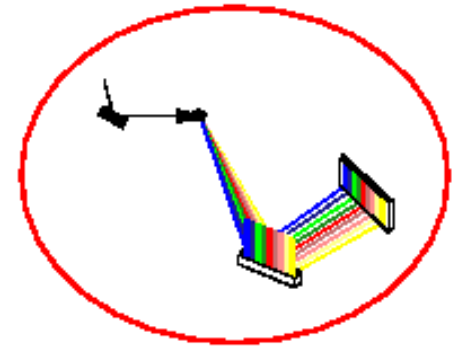


Triple-Axis Spectroscopy

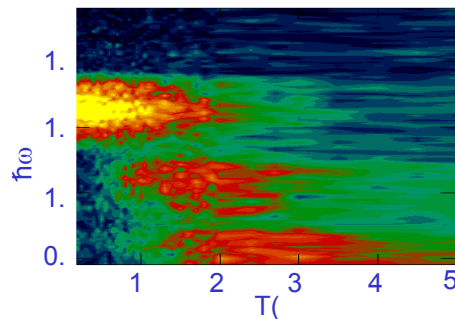
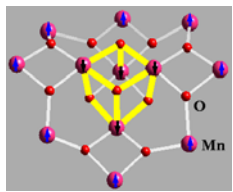
Seung-Hun Lee

Outline

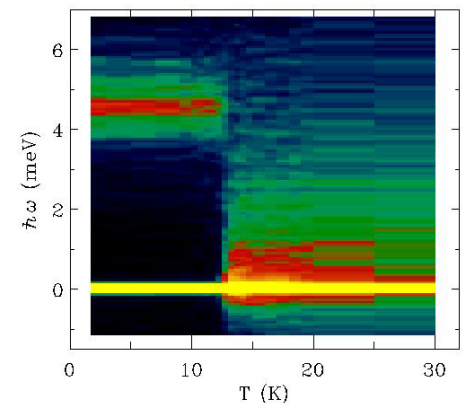
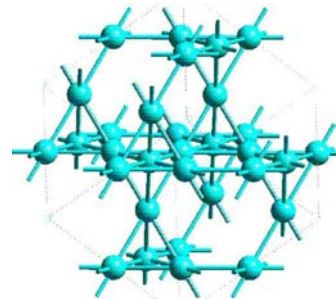
- Basic principles of TAS
- Multiplexing detection modes for TAS
 1. Horizontally focusing mode
 2. Position-sensitive-detector (PSD) mode
- Examples of science utilizing the PSD mode



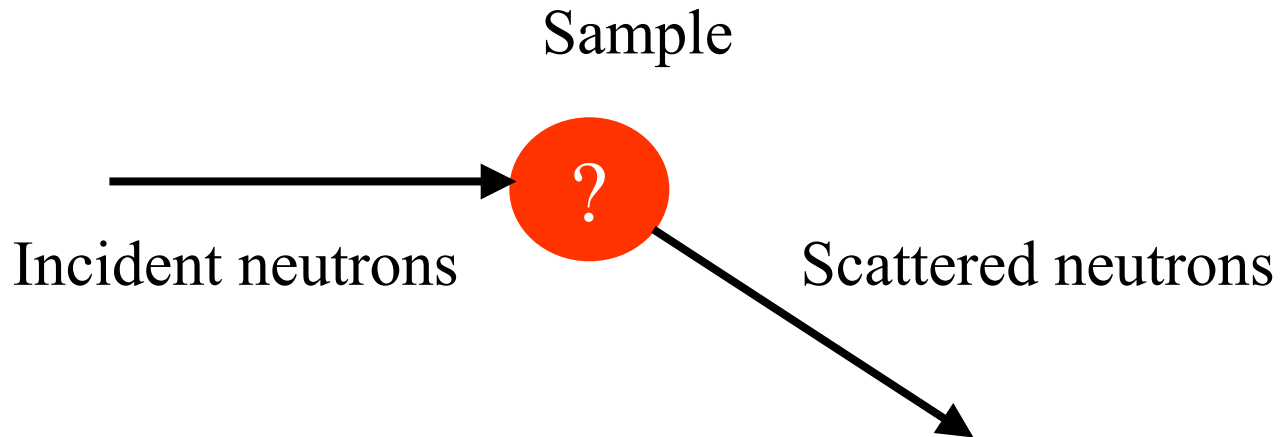
Mn_{12} : Magnetic Molecule



ZnCr_2O_4 : Geometrically Frustrated Magnet



Neutron Scattering



measures scattering cross section as a function of Q and ω

$$\frac{d^2\sigma}{d\Omega d\omega}(\mathbf{Q}, \omega)$$

Neutron Scattering Cross Section

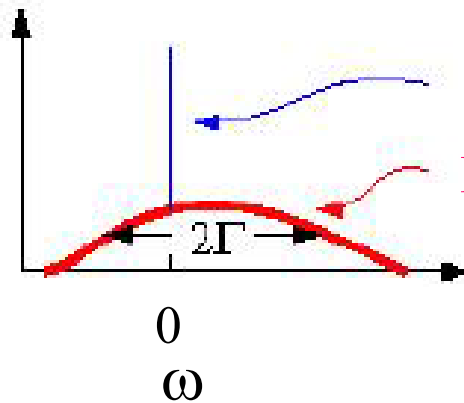
Correlation Function

$$\frac{d^2\sigma}{d\Omega d\omega}$$

Fourier Transform



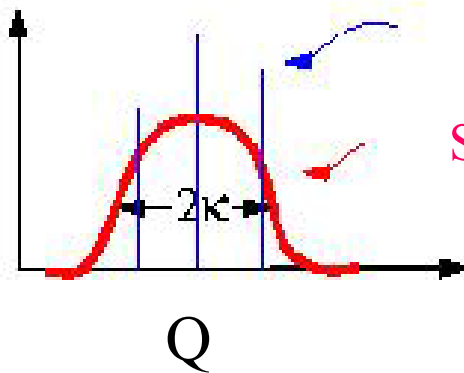
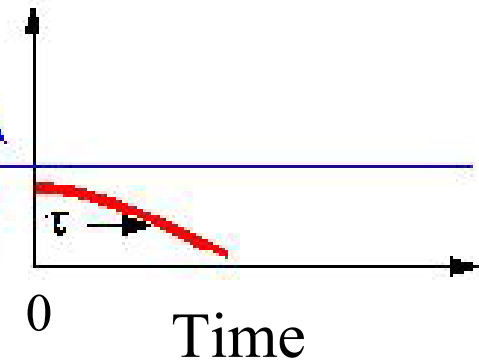
$$\langle S_R(t) S_{R'}(0) \rangle$$



Ordered moment

Fluctuating moment

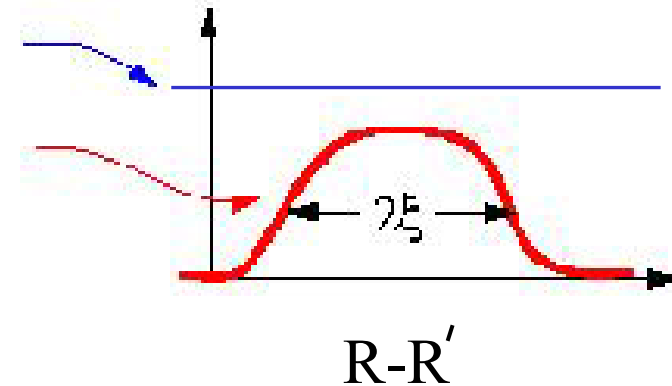
$$\Gamma \sim \hbar/\tau$$



Long range order

Short range order

$$\kappa \sim 1/\xi$$

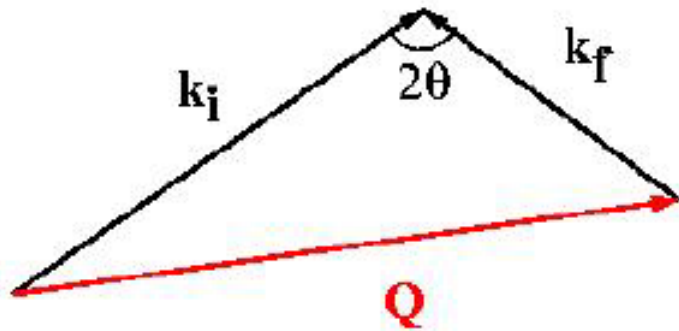


Γ : relaxation time
 κ : intrinsic linewidth

τ : lifetime
 ξ : correlation length

How can we determine Q and ω ?

Scattering triangle : Energy and momentum are conserved in the scattering process

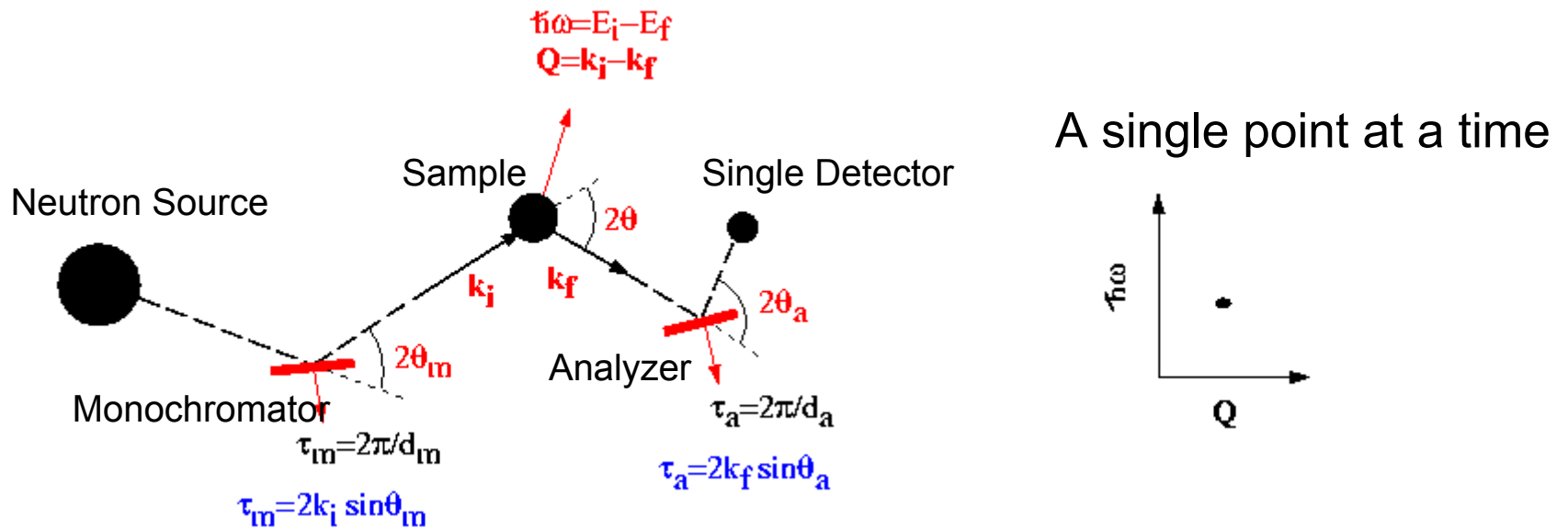


$$Q = k_i - k_f$$
$$\hbar\omega = \frac{\hbar^2}{2m} (k_i^2 - k_f^2)$$

Now, how to determine k_i , k_f , and 2θ ?

- Triple-axis spectroscopy (TAS)
- Time-of-flight spectroscopy (TOF)

Conventional Triple-Axis Spectroscopy (TAS)



TAS is ideally suited for probing small regions of phase space

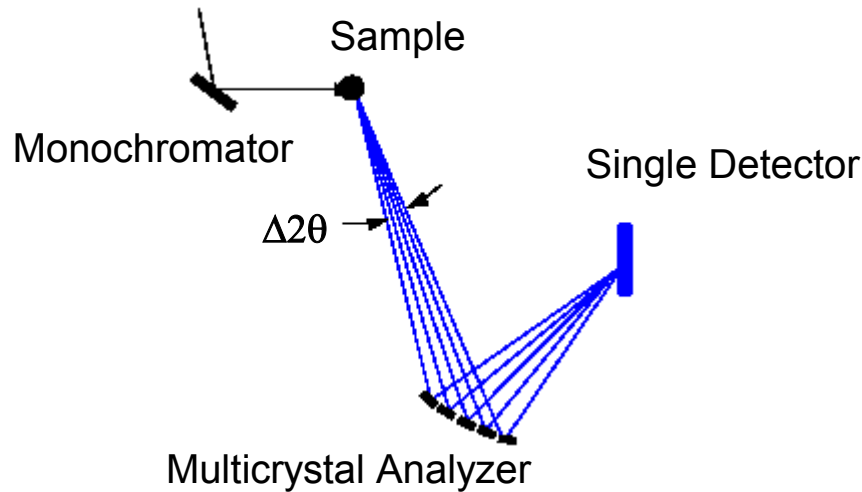
Shortcoming: Low data collection rate



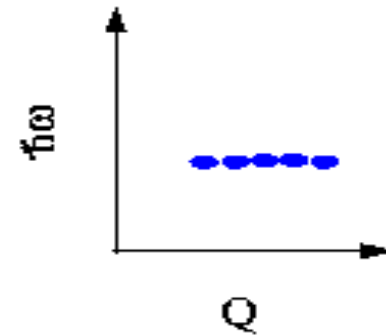
Improvement

Multicrystal analyzer and position-sensitive detector

Horizontally Focusing (HF) Analyzer Mode



Relaxed Q-resolution

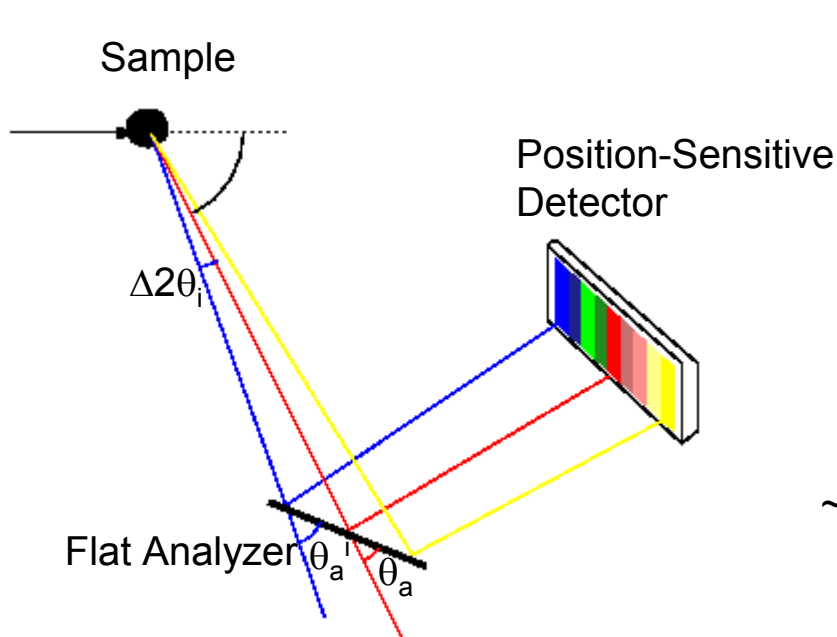


L = distance from sample to HF analyzer
 w_a = total width of HF analyzer

$$\Delta 2\theta = w_a \sin\theta_a / L \sim 9 \text{ degree for } E_f = 5 \text{ meV at SPINS}$$

Useful for studying systems with short-range correlations

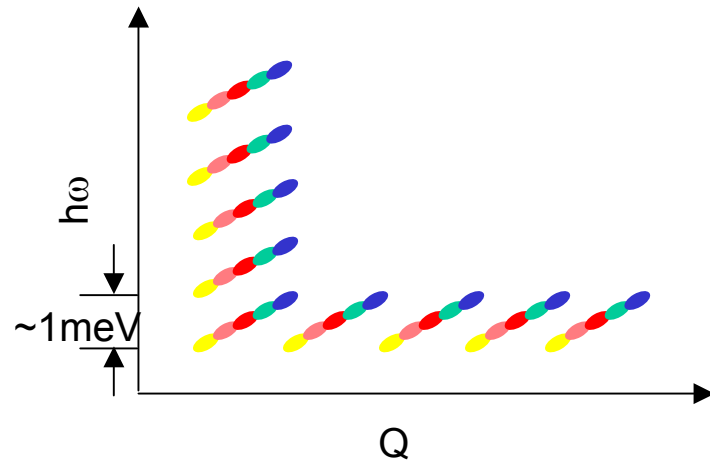
Multiplexing Detection System for TAS



$$\theta_a^i = \theta_a + \Delta 2\theta_i = \theta_a - \text{atan}(x \sin\theta_a / (L + x \cos\theta_a))$$

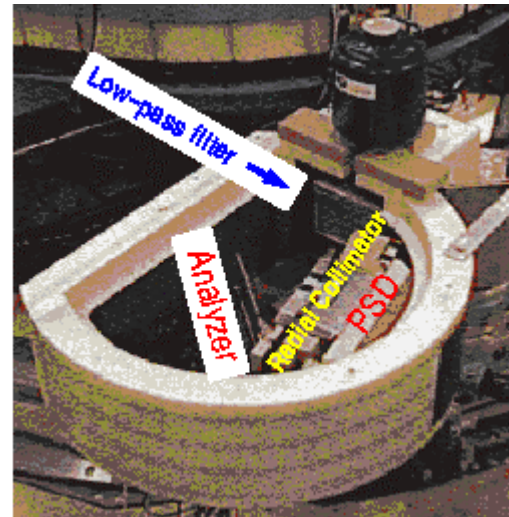
$$k_f^i = \tau_a / 2 \sin\theta_a^i$$

$$Q_i = k_i - k_f^i$$

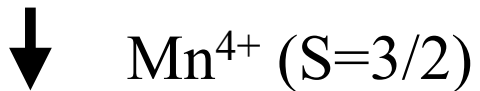
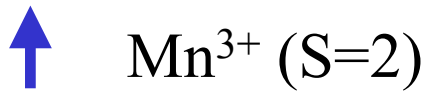
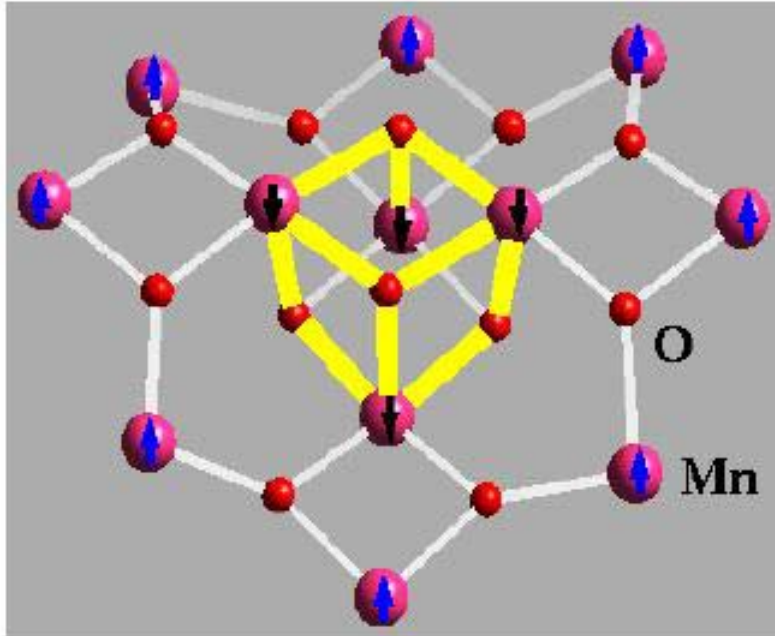


Probes scattering events at different energy and momentum transfers simultaneously

Survey ($h\omega$ - Q) space by changing the incident energy and scattering angle

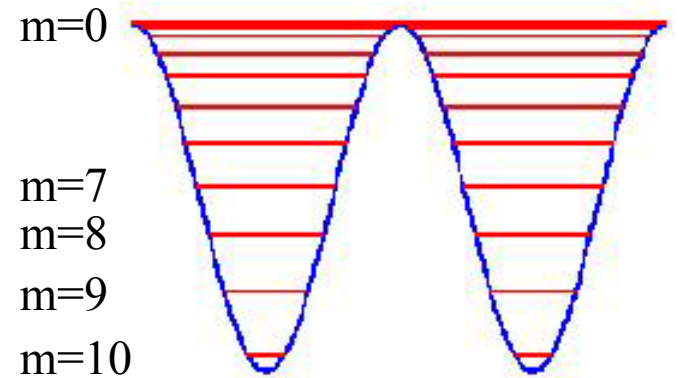


Mn₁₂: Magnetic Molecule

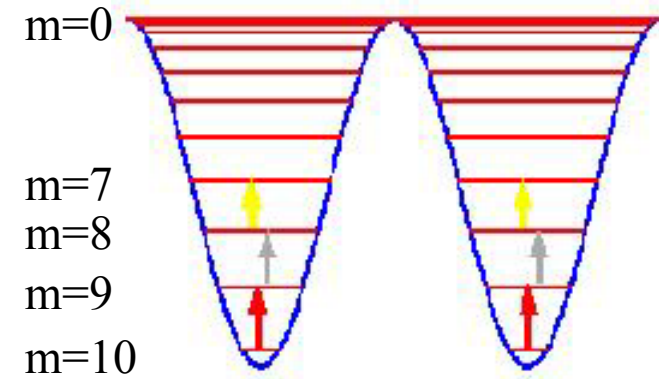
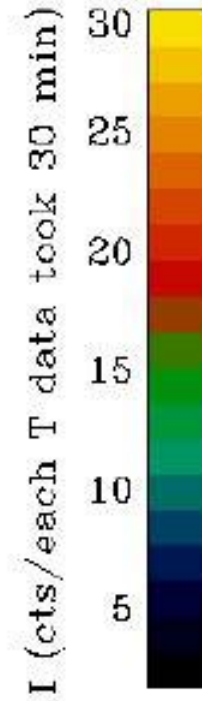
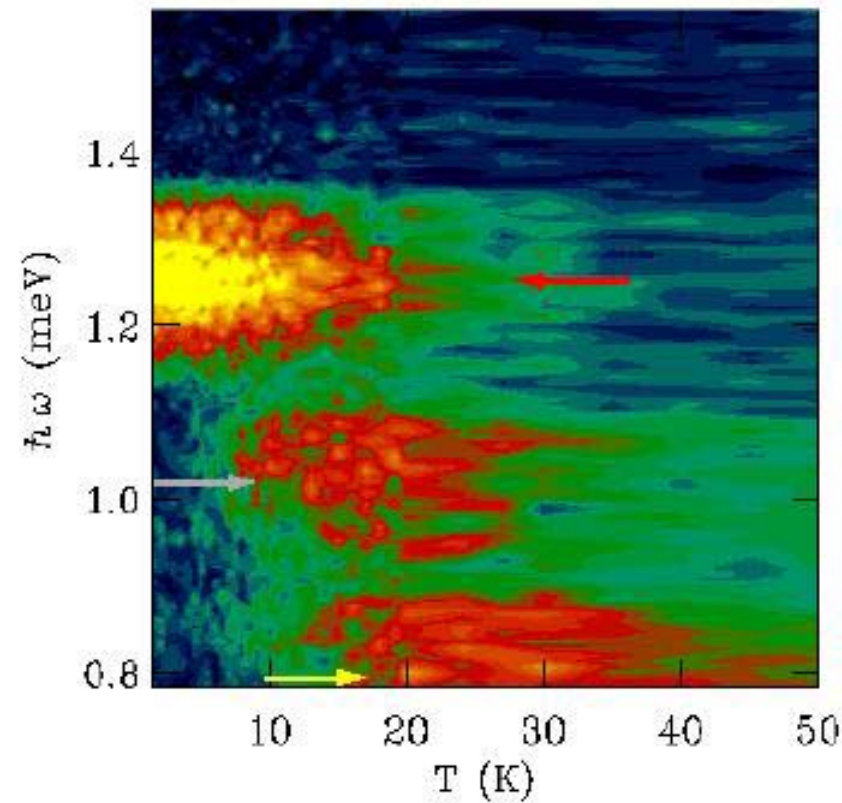


$$S_{\text{tot}} = 10$$

Energy levels : $H = -D S_z^2$

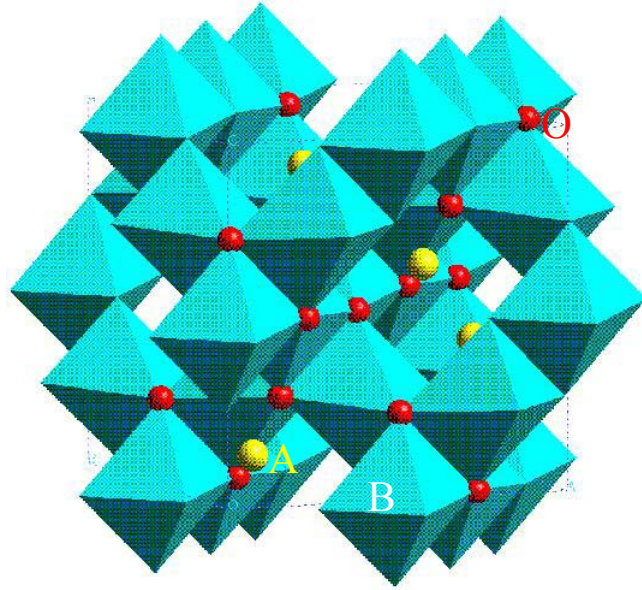


Mn₁₂ Magnetic Molecule : I (T,w) at Q = 1 Å⁻¹



The peaks correspond to transitions between different energy states

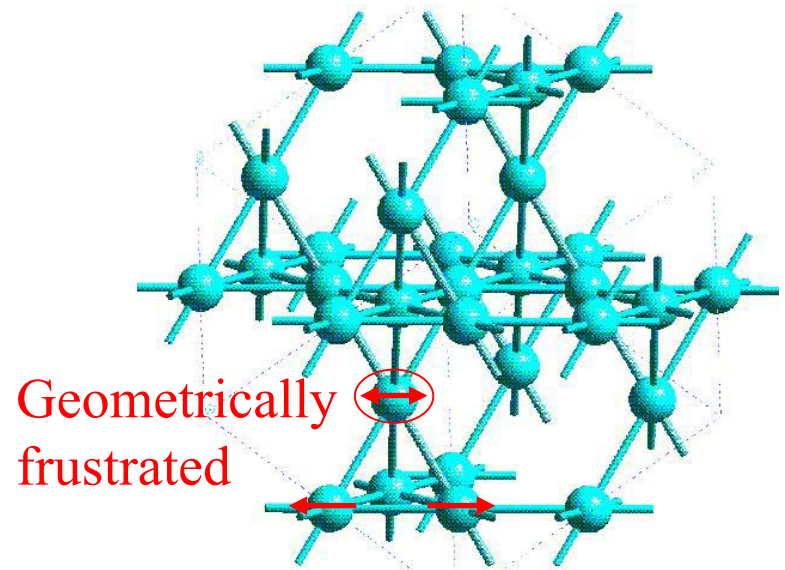
Crystal Structure of Spinel ZnCr_2O_4



**B sites form a network
of corner-sharing tetrahedra
-> Frustrating lattice for
antiferromagnetic spins**

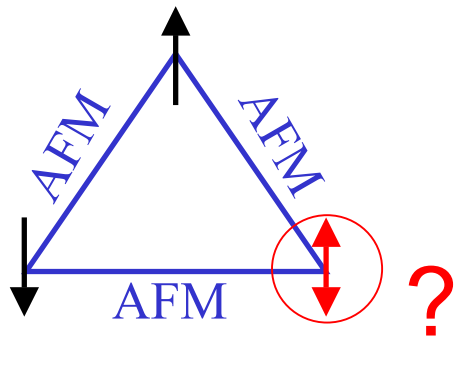
Space group $Fd\bar{3}m$

**B site: the center of O octahedron
with a slight trigonal distortion**



Geometrical Frustration

A simplest example: a Triangle of three antiferromagnetic Ising spins



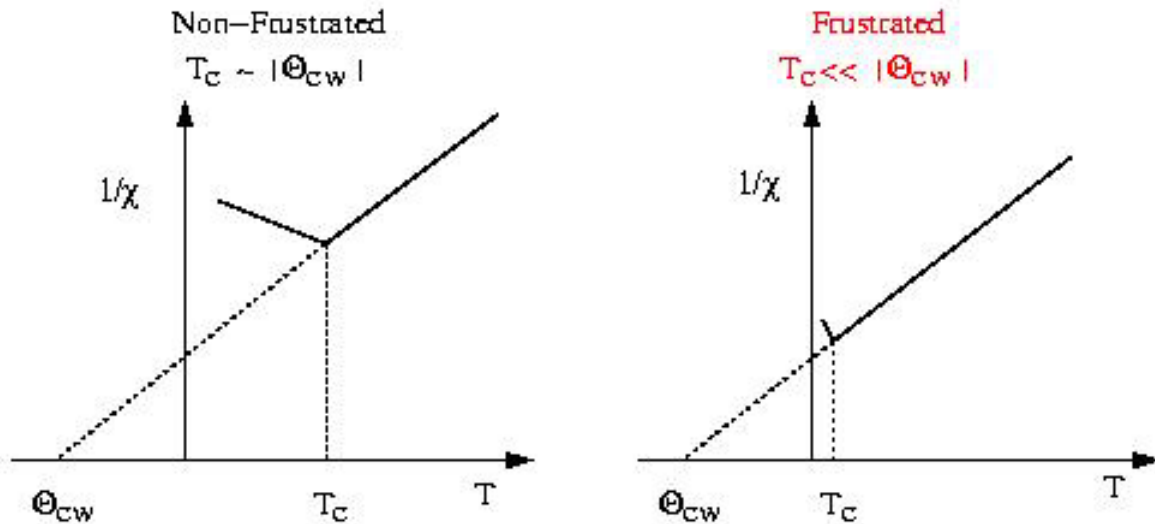
$$H = -J \sum S_i \cdot S_j$$

All exchange interactions can not be satisfied.

$$E = -|J|$$

Geometrical frustration leads to a large degeneracy in the ground state

Effect of Geometrical Frustration

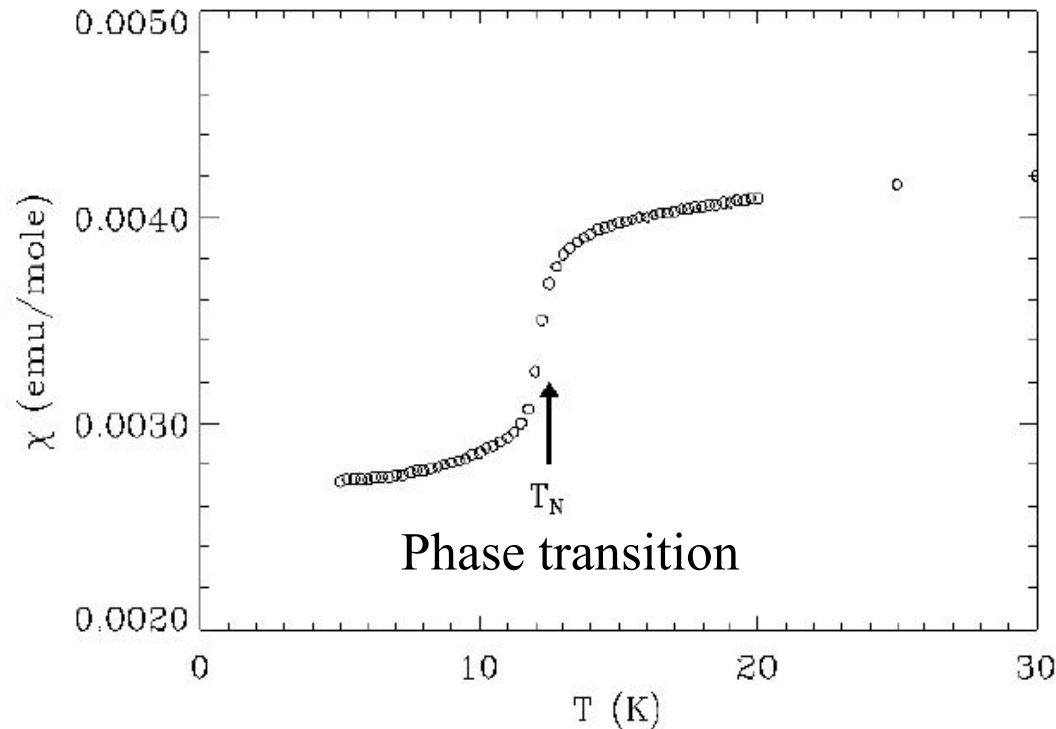


Frustration suppresses the magnetic ordering

A new state of matter ?

Initial Experimental Planning :

Bulk susceptibility from ZnCr_2O_4

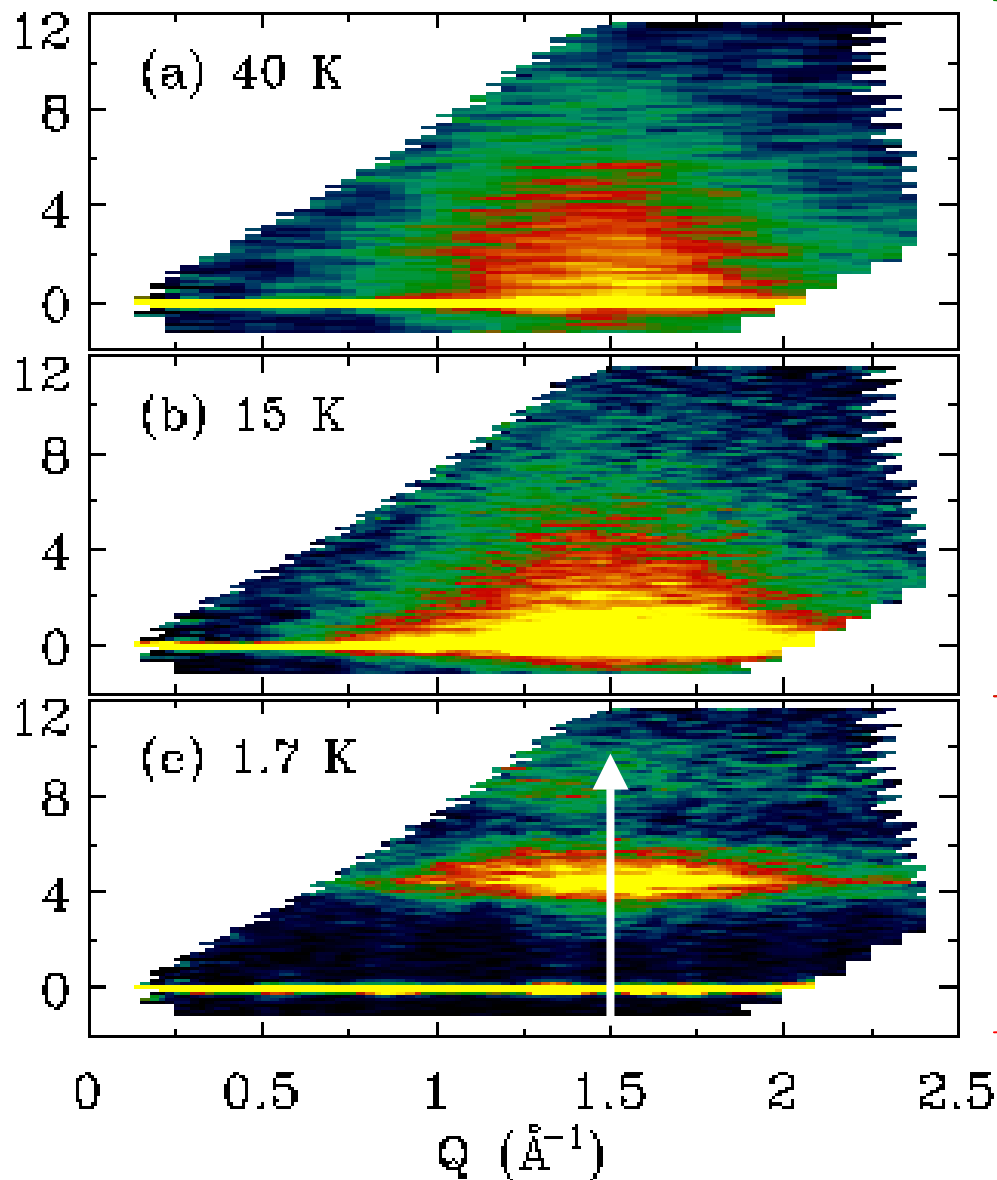


$$\Theta_{CW} = -390 \text{ K}$$

$$T_N = 12.5 \text{ K}$$

How do the spin correlations change through the phase transition ?

Neutron Scattering from ZnCr_2O_4



Paramagnetic
fluctuations in
frustrated AFM

Local spin resonance
in magneto-elastic
LRO phase

Keywords for SPINS Hand-on Experiments

- Triple-axis spectroscopy
 - Multiplexing detection system for a TAS
- Spin correlations
- Magnetic phase transition
- Long range vs Short range order
- Static spin correlations Elastic neutron scattering
- Dynamic spin correlations Inelastic neutron scattering